

# Endogenous Timing with Demand Uncertainty

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This version: November 2011

## Abstract

This paper develops an endogenous timing model where two quantity-setting firms have imperfect information about market demand, and they have an opportunity to solve this uncertainty by carrying out costly market research. It encompasses the classical models of Hamilton and Slutsky (1990) and Sadanand and Sadanand (1996), making their results correspond to two particular cases (namely, high and low market research cost) of our model respectively. Furthermore, we find that endogenous leadership always occurs when market research cost is intermediate, a situation never analyzed so far.

*Keywords:* endogenous timing; market research; endogenous leadership

*JEL classification:* L13; D21; D82

## 1 Introduction

In classical duopoly models, the timing of firms' choices (e.g. production) is exogenously given. For instance, firms are assumed to act simultaneously in Cournot and Bertrand duopolies, and one firm is arbitrarily chosen to take action first in the Stackelberg game or the price leadership model. Of course, the industrial organization literature has long questioned whether and when such settings are realistic, giving rise to a large number of studies which aim to explain the firms' timing choices endogenously. Furthermore, the issue of endogenous timing is important for many other situations beyond oligopoly models (e.g. bargaining<sup>1</sup>). From the purely game-theoretic point of view, it is important to understand which situations give rise to equilibria where simultaneous actions or sequential play, rather than being a modeling assumption, result endogenously.

One of the pioneering works in this area comes from Hamilton and Slutsky (1990) (HS henceforth). They develop two different two-period duopoly models. The first is a game of timing with observable delay, which requires each firm to announce its timing choice first and then to commit to it. For quantity competition, they find a unique pure-strategy SPNE with simultaneous production in the first period. For price competition, there are two pure-strategy SPNE with endogenous leadership. The second of HS' models is a game of timing with action commitment, which makes leadership possible only if a firm produces first and commits to its

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<sup>1</sup>In bargaining models, a stochastic "pie", monetary surplus to be shared, can be interpreted as a downward-sloping demand function for a homogeneous good (see Güth, Ritzberger, and van Damme (2004)).

quantity. In this model, they find two pure-strategy SPNE with endogenous leadership and a pure-strategy SPNE with simultaneous production, independently of whether competition is in prices or in quantities.

Amir and Grilo (1999) reconsider the action commitment model with quantity competition and provide a different set of minimal conditions on demand and cost functions, yielding Stackelberg and Cournot equilibrium respectively. The action commitment model is revisited by van Damme and Hurkens (1999, 2004) as well, but for the purpose of equilibrium selection. Based on the risk dominance considerations and using the tracing procedure, they find that the equilibrium in which the more efficient firm behaves as Stackelberg leader is risk dominant, regardless of whether competition is in prices or in quantities.

A natural extension of HS' models is to consider asymmetric information on market demand. For instance, Sadanand and Sadanand (1996) introduce demand uncertainty into HS' action commitment model. The information about market demand is obscure in the first production period, but automatically becomes clear in the second period. Therefore, the first mover can never be better informed, and there is a trade-off between leading the market and knowing more. In the end, Cournot equilibria appear if either there is no market uncertainty or it is sufficiently large, while Stackelberg equilibria survive if the uncertainty is small.

Also based on HS' models with information uncertainty, Güth, Ritzberger, and van Damme (2004) consider the timing choices in a bargaining game. In their models, two parties have to divide a pie whose size is uncertain in the first period. In the action commitment model, they show that if the uncertainty is sufficiently small, sequential play will appear in the equilibrium. In the model of observable delay, however, if the uncertainty is small, both parties would commit to demand before the accurate information is revealed; if the uncertainty is large, wait and see is the choice for both parties in the equilibrium.

Built on the same idea as HS' action commitment model, Güth and Güth (2001) develop a model about capacity and price determination, where two firms, facing uncertain production costs, have to decide when to choose capacities and when to choose prices. Although an exhaustive analytical result is not available, numerical examples show that either Cournot or non-Cournot result could happen, depending on the cost distributions.

Another class of models allow the better-informed firm to move in the first period, hence bringing about signaling problems. The works in this direction include Mailath (1993), Daughety and Reinganum (1994) and Normann (2002).

We briefly single out a few other relevant contributions to the endogenous timing literature. Saloner (1987) and Pal (1991) allow firms to produce in both periods and the output levels in period 1 become public information before production at period 2. Maggi (1996) analyzes a two-period investment game based on the same structure. Pal (1998) studies the endogenous timing problem of a mixed oligopoly, meaning an oligopoly with a welfare-maximizing public firm and several profit-maximizing private firms. A related paper from Lu (2006) introduces foreign competitors into the endogenous timing model for a mixed oligopoly. Hirokawa and Sasaki (2001) consider an infinite horizon model where firms have to decide in which period to enter and then commit to an output level for all future periods. Ishibashi (2008) discusses the endogenous timing problem for collusive price leadership with capacity constraints. Finally, Berninghaus and Güth (2004) consider the timing choices of threats of two parties in a bargaining problem.

In this paper, we explore firms' timing choices in a quantity-setting duopoly model with stochastic demand and costly market research. The innovation of this paper, in our view, is that not only the timing of market decisions is endogenous, but also the resolution of

demand uncertainty. In the existing literature, information acquisition is always assumed to be costless (see e.g. Güth, Ritzberger, and van Damme (2004) and Sadanand and Sadanand (1996)). When there is demand uncertainty, the accurate information on market demand is automatically revealed to firms after waiting for one period. In this paper, however, we assume that firms have to decide whether or not to invest effort (costing both time and money), to acquire accurate information on market demand. We believe it is a more realistic assumption.

The basic structure of the model is based on HS' endogenous timing models. The structure of our first model corresponds to HS' game of action commitment. In our case, two firms have to decide whether they will commit to certain quantity in the first period, carry out market research, or just wait and see. Such a modeling structure applies to the situations where irrevocable commitments are related to actions. For instance, firms with strict capacity constraints (e.g. steel production) would like to commit to their output levels, because substantial costs will be incurred when adjusting the production capacities. If firms sell their goods through retailers, the demands are often predetermined in the contract, hence lacking adjustment flexibility as well (see e.g. Hirokawa and Sasaki (2001)). For sales of durable consumption goods, e.g. automobiles, retailers may post prices, also representing a commitment (see e.g. Güth, Ritzberger, and van Damme (2004)). Our second model is built on HS' game of observable delay. This framework applies to the situations where players only announce when actions will be taken, but not the action themselves. For instance, shopkeepers know that retailers in mail-order distribution systems have to decide prices when printing catalogues, but the prices are unknown until the catalogues are published (see e.g. Güth, Ritzberger, and van Damme (2004)). In our case, there is an initial stage, where firms will announce whether they will produce in the first period, carry out market research, or just wait and see.

As to the timing of information acquisition, the model is similar to Güth, Ritzberger, and van Damme (2004) and Sadanand and Sadanand (1996), in the sense that accurate information of market demand becomes available only at period 2, therefore, there is no signaling problem.<sup>2</sup> The main difference concerns information acquisition. In this paper, obtaining information is *costly*. In view of the widespread existence of market research departments in most firms and large number of independent market research companies, this assumption is probably more realistic than the costless revelation of information. Hence, in this aspect, our model is related to Daughety and Reinganum (1994), wherein firms have to pay for information. However, there is an important difference in the nature of the market research process. In Daughety and Reinganum (1994)'s model, information is bought from market research institutes, hence it is assumed to be an activity requiring only negligible time compared to production. In this paper, however, we consider market research to be a time-consuming activity, requiring an amount of time comparable with that necessary for production activities. This assumption is sensible for the following reasons. A professional and accurate market research is not a simple task. It normally includes objective setting, planning of investigation procedure, data collection, data analysis, reporting and decision making in the end (see Hague (2002)). Sometimes, even one step in the whole procedure takes a long time, for instance, interviewing a large number of potential consumers. For firms facing a global market, obtaining accurate market information becomes even more difficult, due to the huge economic, cultural and political differences in different countries and regions. Therefore, the time involved in

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<sup>2</sup>Abstracting from signaling considerations will allow us to encompass HS' seminal model as a particular case.

market research is significant, which gives rise to a choice between starting production right away or performing market research first.

The timing choices of both firms depend on a trade-off. Each firm can either carry out market research in the first period to obtain accurate market information, or produce first aiming to obtain a “first mover advantage”. We will show that the qualitative characteristics of the subgame-perfect Nash equilibria are determined by the combined effects of market conditions (measured by the expectation and variance of market capacity), technology (measured by production costs), and market research costs. For the model featured by action commitment, if the market research cost  $K$  is too high relative to the variance of market capacity, market research never plays a role. This case encompasses HS’ model of action commitment as a particular case. The intuition is simply that it does not pay to eliminate the uncertainty. For an intermediate value of  $K$ , we find two SPNE with endogenous leadership, independently of production costs. This is a relatively clear-cut case, in which one firm takes the trade-off and receives more information but becomes a follower, and the other firm obtains the first-mover advantage but pays the price of facing an uncertain demand.

If  $K$  is low enough relative to the variance of market capacity (the extreme case  $K = 0$  corresponds to Sadanand and Sadanand (1996)), the situation is more complex. For given market conditions, there are two SPNE exhibiting endogenous leadership, provided the production cost of both firms are low enough. If the production cost of one firm is low enough but that of the other one is very high, then there is a unique SPNE with the more efficient firm as a leader. If production costs of both firms are too high, there is a SPNE involving simultaneous production in the second period. If market conditions becomes more favorable (higher expectation and lower variance of the market capacity), the SPNE with endogenous leadership survives even if the production of the leader is less efficient. The appearance of the SPNE with simultaneous production also requires much higher production costs of both firms. The converse is true if market conditions are unfavorable.

For the model with observable delay, if  $K$  is high, both firms will produce as in a Cournot duopoly in the first period. If  $K$  is low or intermediate, both the Cournot outcome in the first period and the Stackelberg outcome with market research can be SPNE, depending on market research cost, production costs, and market conditions.

## 2 The Model with Action Commitment

We consider a quantity-setting duopoly in a market with stochastic demand. The inverse demand function is given by  $P(Q) = a - Q$  (i.e. we normalize the slope of market demand to 1, as in Daughety and Reinganum (1994) and Sadanand and Sadanand (1996)). Market capacity, given by the parameter  $a > 0$ , is a random variable with support contained in an interval  $[a^L, a^H]$ , assumed to have expectation  $E[a]$  and variance  $V[a] \neq 0$ . In particular,  $a$  might be a continuous random variable or take only a finite number of values. Firm  $i$  ( $i = 1, 2$ ) has a constant marginal cost  $c_i$ , which satisfies

$$0 < c_1 \leq c_2 < a^L. \quad (1)$$

To simplify the analysis, we also assume that

$$c_2 < \frac{1}{3}(2a^L - E[a] + 2c_1) \quad (2)$$

to ensure that all the quantities used in the model are strictly positive.<sup>3</sup>

There are two time periods.<sup>4</sup> The (unknown) market demand does not change during the two periods, or, equivalently, it is realized at the end of the second period. At the beginning of the first period, firms have commonly known prior beliefs on  $a$  as stated above and can choose among three different choices: (i) to produce a certain quantity; (ii) to carry out market research; and (iii) to wait.

If a firm decides to produce a certain quantity in the first period, it observes neither the realized market demand nor the choice of its opponent. We assume that production is final, that is, a firm which produces in the first period cannot produce additional units in the second period.<sup>5</sup>

If a firm decides to carry out market research, it will find out the realization of market capacity at a cost  $K \geq 0$ , and observe the first period's choice of its opponent. In the second period, the firm will choose a quantity with full knowledge of the market demand. We say that this firm has perfect information on market demand. If a firm decides simply to wait, it observes its opponent's first-period choice, but cannot update its market information. In the second period, it has to choose a quantity without additional knowledge of the market demand. We say that this firm has imperfect information on market demand.

Since market research completely reveals the information on market conditions, the value of market research is simply the difference of profits a firm obtains under perfect and imperfect information, given the action of its opponent. Firms will compare this value with  $K$ , and then decide whether or not to carry out market research.<sup>6</sup>

In short, information on the market demand is updated only after market research and each firm produces in one period only. Thus our model is quite different from two-period production models as Saloner (1987), where firms can accumulate outputs in two periods. It is an extension of HS' game of timing with action commitment allowing for stochastic market demand and market research.

Formally, the model gives rise to an extensive-form game. The set of players is  $I = \{1, 2\}$ . For each firm  $i \in \{1, 2\}$ , let  $M_i$  denote the choice of carrying out market research and  $W_i$  the choice of waiting in the first period. The action of firm  $i$  in the first period is denoted by

$$s_i^1 \in S_i^1 = \mathbb{R}^+ \cup \{M_i, W_i\},$$

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<sup>3</sup>This inequality guarantees the perfect-information Stackelberg follower quantity of firm 2 to be positive. It also ensures that all other quantities used in the analysis are positive.

<sup>4</sup>A period is treated as an indivisible time unit in which firms can start and finish their actions. A detailed discussion about the effect of time length on strategic timing choices is in Pacheco-de-Almeida and Zemsky (2003), where each period is further subdivided in  $T$  subunits.

<sup>5</sup>Thus, in this model, firms producing in the first period *commit* to a quantity. Commitment issues can of course be discussed at length, but are not very pertinent to the issue of endogenous timing. Henkel (2002) studies the issue of commitment in a model of alternating moves (i.e. exogenous timing) where a player announces a decision and fixes a deviation cost; this player can revise the initial decision after a second player acts, by paying the deviation cost. In equilibrium, the chosen cost becomes a device to make the commitment credible. If actions are strategic substitutes, in the unique SPNE player 1 announces the Stackelberg leader action and a large deviation cost, player 2 responds with the Stackelberg follower action, and player 1 does not revise his action. Player 1 obtains the so-called "1.5th mover advantage".

<sup>6</sup>Ponssard (1976) discusses the value of information in competitive situations in the case where an experiment fully reveals the state of nature. It is, of course, not completely realistic that market research resolves all uncertainty about demand. More generally, one could investigate cases where market research reduces more or less the variance, e.g. by producing a more or less noisy signal  $\hat{a}$ . We stick to our assumption for the purpose of simplicity and tractability.

and the second period decision is given by a mapping

$$s_i^2 : ([a^L, a^H] \cup \{W_i\}) \times (\mathbb{R}^+ \cup \{M_{-i}, W_{-i}\}) \rightarrow \mathbb{R}^+.$$

For example,  $s_i^2(a|q)$  is the output level of firm  $i$  in period two, given that in the first period this firm carried out market research revealing market capacity  $a$ , but its opponent produced  $q$ . Analogously,  $s_i^2(W_i|M_{-i})$  is the output level of firm  $i$  in period two, given that in the first period this firm decided to wait, but its opponent carried out market research.

Denote by  $S_i^2$  the set of all functions  $s_i^2$  as above. The strategy set of firm  $i$  is given by  $S_i = S_i^1 \times S_i^2$ , with typical element  $s_i = (s_i^1, s_i^2)$ . The payoff function of firm  $i$  is  $\pi_i : S_i \times S_{-i} \rightarrow \mathbb{R}^+$ .

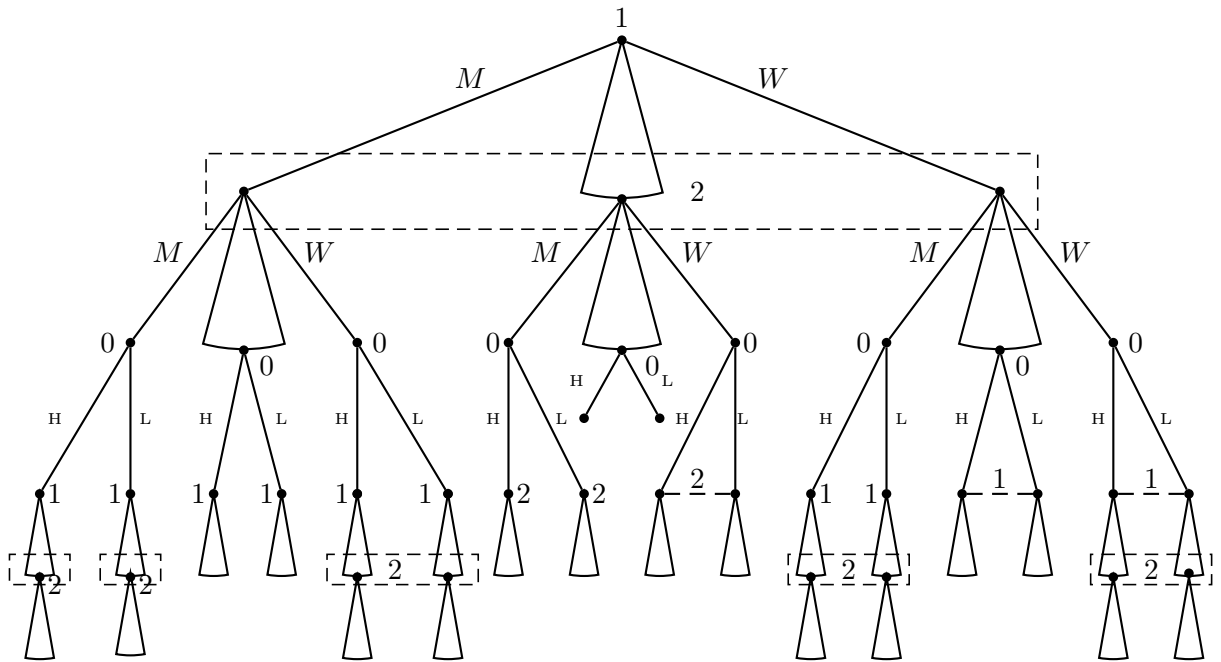


Figure 1: The extensive form when  $a$  can only take two values. Dashed lines and boxes indicate information sets.

Figure 1 shows the extensive-form of this game for the particular case where the random variable  $a$  follows a Bernoulli distribution, with  $a = a^H$  with probability  $p$  and  $a = a^L$  with probability  $1 - p$ .

In studying the extensive-form game, we make the modelling decision to have nature move at the beginning of the second period. This does not change the economic model at all, but generates an extensive-form game, in which every possible strategic situation in the second period corresponds to a proper subgame. Thus the appropriate equilibrium concept is simply Subgame-Perfect Nash Equilibrium (SPNE). An alternative treatment following Harsanyi's transformation would be to have nature move at the beginning of the first period. Under such a setup, many second-period situations would fail to give rise to proper subgames and

we would have to resort to the use of Perfect Bayesian Equilibrium (PBE) as a solution concept. This added complication is void of economic content. A PBE consists of a belief system and a strategy profile, but the belief system in this model is trivial, since the beliefs on market capacity are exogenously given. Given these beliefs, one would use sequential rationality to derive the equilibrium strategy profiles, which are identical with those of the SPNE in the first treatment. Thus our choice allows us to greatly simplify the notation.

### 3 Equilibrium Analysis

#### 3.1 Equilibrium Behavior in the Second Period

We first determine both firms' decisions in the second period; that is, we find the Nash Equilibria in each proper subgame.

**Two informed firms.** If both firms choose market research in the first period, the second-period subgames (one for each possible realization of  $a$ ) are such that both firms produce simultaneously with perfect information on the market demand. The Nash equilibrium of one of these subgames corresponds to the Cournot-Nash equilibrium of the perfect-information duopoly. The equilibrium quantity of each firm  $i$  for each state  $a \in [a^L, a^H]$  is denoted by  $q_i^c(a)$ . that is, the equilibrium strategy must prescribe

$$s_i^2(a|M_{-i}) = q_i^c(a) = \frac{1}{3}(a - 2c_i + c_{-i}), \quad i = 1, 2 \quad (3)$$

which is always a strictly positive quantity.<sup>7</sup>

**Two uninformed firms.** If both firms choose to wait, neither of them is informed on the realized market demand. This leads to a second-period (Bayesian) subgame where both firms produce simultaneously with imperfect information on the market demand. The Nash equilibrium corresponds to the Cournot-Nash equilibrium of the imperfect-information duopoly, where the equilibrium quantity of each firm  $i$  is given by  $q_i^c(E[a])$ . Thus, the equilibrium strategies are such that

$$s_i^2(W_i|W_{-i}) = q_i^c(E[a]) = \frac{1}{3}(E[a] - 2c_i + c_{-i}), \quad i = 1, 2. \quad (4)$$

**One informed firm.** If firm  $i$  choose to carry out market research and firm  $-i$  to wait, in the second-period subgame both firms produce simultaneously with asymmetric information. In equilibrium, the informed firm conditions on the realization of  $a$ , but the uninformed firm does not. Denote the equilibrium quantity of the informed firm by  $q_i^{Ic}(a)$ . It is easy to show that

$$s_i^2(a|W_{-i}) = q_i^{Ic}(a) = \frac{1}{6}(3a - E[a] - 4c_i + 2c_{-i}), \quad \forall a \in [a^L, a^H], \quad i = 1, 2 \quad (5)$$

which is always strictly positive.<sup>8</sup> From the point of view of the uninformed firm  $-i$ , the expected equilibrium output of firm  $i$  is  $q_i^c(E[a])$ . Thus the equilibrium quantity of the

<sup>7</sup>For the more efficient firm's quantity  $q_i^c(a)$ , this follows from  $0 < c_1 \leq c_2 < a^L$ . For the other firm,  $q_2^c(a) > 0 \forall a$  if  $c_2 < \frac{1}{2}(a^L + c_1)$ . This condition follows from the assumption  $c_2 < \frac{1}{3}(2a^L - E[a] + 2c_1)$ , because  $\frac{1}{2}(a^L + c_1) - \frac{1}{3}(2a^L - E[a] + 2c_1) = \frac{1}{6}(2E[a] - a^L - c_1) > 0$ .

<sup>8</sup>For the more efficient firm,  $q_1^{Ic}(a) > 0$  if  $c_1 < \frac{1}{4}(3a^L - E[a] + 2c_2)$ . This follows from the assumptions  $c_1 \leq c_2 < \frac{1}{3}(2a^L - E[a] + 2c_1)$  and the fact that  $\frac{1}{3}(2a^L - E[a] + 2c_1) - \frac{1}{4}(3a^L - E[a] + 2c_2) = -\frac{1}{12}[(6c_2 - 6c_1) + (a^L + E[a] - 2c_1)] < 0$ . For the less efficient firm,  $q_2^{Ic}(a) > 0$  if  $c_2 < \frac{1}{4}(3a^L - E[a] + 2c_1)$ . This follows from the assumption  $c_2 < \frac{1}{3}(2a^L - E[a] + 2c_1)$ , because  $\frac{1}{3}(2a^L - E[a] + 2c_1) - \frac{1}{4}(3a^L - E[a] + 2c_1) = -\frac{1}{12}(a^L + E[a] - 2c_1) < 0$ .

uninformed firm is equal to  $q_{-i}^c(E[a])$ . Hence, in equilibrium

$$s_i^2(W_i|M_{-i}) = q_i^c(E[a]), \quad i = 1, 2. \quad (6)$$

**A leader and an informed follower.** If firm  $i$  chose to carry out market research and firm  $-i$  to produce a certain quantity, in the corresponding second-period subgame only firm  $i$  plays, choosing a certain quantity knowing both the demand and the quantity of its opponent. The equilibrium strategy of firm  $i$  is thus to adopt a best response to its opponent's quantity. That is,

$$s_i^2(a|s_{-i}^1) = \max\{0, \frac{1}{2}(a - c_i - s_{-i}^1)\}, \quad \forall s_{-i}^1 \in \mathbb{R}^+, \quad i = 1, 2. \quad (7)$$

**A leader and an uninformed follower.** If firm  $i$  chose to wait and firm  $-i$  to produce a certain quantity, in the corresponding second-period subgame only firm  $i$  plays, choosing a certain quantity knowing the quantity of its opponent but not the demand. The equilibrium strategy is

$$s_i^2(W_i|s_{-i}^1) = \max\{0, \frac{1}{2}(E[a] - c_i - s_{-i}^1)\}, \quad \forall s_{-i}^1 \in \mathbb{R}^+, \quad i = 1, 2. \quad (8)$$

Lemma 1 summarizes our computations.

**Lemma 1.** *In any SPNE, if a firm  $i = 1, 2$  decides not to produce in the first period, in the second period its action  $s_i^2$  must be such that*

$$s_i^2(a, s_{-i}^1) = \begin{cases} \frac{1}{3}(a - 2c_i + c_{-i}) & \text{if } s_{-i}^1 = M \\ \frac{1}{6}(3a - E[a] - 4c_i + 2c_{-i}) & \text{if } s_{-i}^1 = W \\ \frac{1}{2}(a - c_i - s_{-i}^1) & \text{if } s_{-i}^1 \in \mathbb{R}^+ \end{cases} \quad (9)$$

for all  $a \in [a^L, a^H]$ , and

$$s_i^2(W_i, s_{-i}^1) = \begin{cases} \frac{1}{3}(E[a] - 2c_i + c_{-i}) & \text{if } s_{-i}^1 = M \text{ or } W \\ \frac{1}{2}(E[a] - c_i - s_{-i}^1) & \text{if } s_{-i}^1 \in \mathbb{R}^+ \end{cases} \quad (10)$$

### 3.2 Equilibrium Behavior in the First Period

Let  $\bar{s}_i^2 \in S_i^2$  be the functions defined in Lemma 1. Taking them as given (i.e. applying backwards induction), the extensive-form game can be simplified to a reduced normal-form game in which both firms only have to decide (in the first period) whether to produce, carry out market research, or wait. We would like to emphasize again that ‘‘produce in the first period’’ is not a single choice, but merely a simplified expression that we use to indicate that the firm chooses some quantity in  $\mathbb{R}^+$ . Hence in the reduced normal-form game, the choice set of each firm is  $\mathbb{R}^+ \cup \{M_i, W_i\}$ . Table 1 shows the expected payoffs for a firm<sup>9</sup> in this reduced normal-form game, where  $q_i$  stands for a quantity in  $\mathbb{R}^+$  for both  $i \in \{1, 2\}$ .

We use this reduced normal-form game to find the possible pure-strategy equilibria.<sup>10</sup> We proceed as follows. First we find equilibrium candidates, e.g., assuming that there is an equilibrium where both firms produce in the first period, we determine what the optimal production plans should be. Later on we will check whether these candidate equilibria are

<sup>9</sup>Since the game is symmetric, only firm  $i$ 's payoff is shown in the table.

<sup>10</sup>In mixed-strategy equilibria, firms randomize between producing first, carrying out market research, and waiting. Thus, there are no clear-cut timing choices which could be used to explain the appearance of endogenous leadership or simultaneous production.



|       | $q_{-i}$                                 | $M_{-i}$                                     | $W_{-i}$  |
|-------|--|--|---|
| $q_i$ | $(E[a] - q_i - q_{-i} - c_i)q_i$         | $\frac{1}{2}(E[a] - q_i - 2c_i + c_{-i})q_i$ | $\frac{1}{2}(E[a] - q_i - 2c_i + c_{-i})q_i$        |
| $M_i$ | $\frac{1}{4}E[(a - c_i - q_{-i})^2] - K$ | $\frac{1}{9}E[(a - 2c_{-i} + c_i)^2] - K$    | $\frac{1}{36}E[(3a - E[a] - 4c_i + 2c_{-i})^2] - K$ |
| $W_i$ | $\frac{1}{4}(E[a] - c_i - q_{-i})^2$     | $\frac{1}{9}(E[a] - 2c_i + c_{-i})^2$        | $\frac{1}{9}(E[a] - 2c_i + c_{-i})^2$               |

Table 1: The Reduced Normal-Form Game

actually equilibria, e.g., whether firms have an incentive to deviate to either wait or carry out market research.

**Both firms research.** When both firms choose to carry out market research, the equilibrium candidate corresponds to the Cournot-Nash equilibrium quantities with perfect information. In each state, each firm  $i$  will produce  $q_i^c(a)$  and receive net profits  $\pi_i^c(a) - K$ , where

$$\pi_i^c(a) = \frac{1}{9}(a - 2c_i + c_{-i})^2, \forall i \in \{1, 2\} \quad (11)$$

Then the expected net profit of firm  $i$  is  $E[\pi_i^c(a)] - K$ .

**Both firms produce.** When both firms choose production, the unique equilibrium candidate is the profile where each firm produces  $q_i^c(E[a])$ . Expected profits are then  $\pi_i^c(E[a])$ , that is,

$$\pi_i^c(E[a]) = \frac{1}{9}(E[a] - 2c_i + c_{-i})^2. \quad (12)$$

**Both firms wait.** When both firms choose to wait, the equilibrium candidate again involves the Cournot-Nash equilibrium quantities with imperfect information. Each firm  $i$  will produce  $q_i^c(E[a])$  and receive expected profits  $\pi_i^c(E[a])$ . The only difference with the previous case is that these quantities are actually produced in the second period.

**Production vs. Research.** When firm  $i$  chooses to produce and firm  $-i$  carries out market research, the unique equilibrium candidate corresponds to the Stackelberg equilibrium where the follower has superior information. We denote the equilibrium quantity of the uninformed leader by  $q_i^\ell$  and that of the informed follower by  $q_{-i}^f(a)$ .

$$q_i^\ell = \frac{1}{2}(E[a] - 2c_i + c_{-i}), \quad (13)$$

$$q_{-i}^f(a) = \frac{1}{4}(2a - E[a] - 3c_{-i} + 2c_i). \quad (14)$$

We also denote  $\pi_i^\ell$  the expected profit of the leader and  $\pi_{-i}^f(a)$  the gross profit of the informed follower in state  $a$ . That is,

$$\pi_i^\ell = \frac{1}{8}(E[a] - 2c_i + c_{-i})^2, \quad (15)$$

$$\pi_{-i}^f(a) = \frac{1}{16}(2a - E[a] - 3c_{-i} + 2c_i)^2. \quad (16)$$

Hence the expected net profit of the informed follower  $-i$  is  $E[\pi_{-i}^f(a)] - K$ .

**Production vs. Waiting.** When firm  $i$  chooses to produce and firm  $-i$  to wait, the equilibrium candidate corresponds to the Stackelberg equilibrium with imperfect information. The uninformed Stackelberg leader will produce  $q_i^\ell$  and receive expected profits  $\pi_i^\ell$ . The uninformed follower will produce  $q_{-i}^f(E[a])$  and receive expected profits  $\pi_{-i}^f(E[a])$ . That is,

$$\pi_{-i}^f(E[a]) = \frac{1}{16}(E(a) - 3c_{-i} + 2c_i)^2 \quad (17)$$

**Research vs. Waiting.** When firm  $i$  carries out market research and firm  $-i$  chooses to wait, the informed firm  $i$  will produce  $q_i^{Ic}(a)$  for each state  $a \in \{1, 2\}$  and firm  $-i$  will produce  $q_{-i}^c(E[a])$ . The gross profit of the informed firm in each state is denoted by  $\pi_i^{Ic}(a)$ .

$$\pi_i^{Ic}(a) = \frac{1}{36}(3a - E[a] - 4c_i + 2c_{-i})^2 \quad (18)$$

The expected net profit of this firm is  $E[\pi_i^{Ic}(a)] - K$ . The expected profit of the uninformed firm is equal to  $\pi_{-i}^c(E[a])$ .

Table 2 shows the payoffs of the equilibrium candidates.

|       | $q_2$                           | $M_2$                                  | $W_2$                                 |
|-------|---------------------------------|--|---------------------------------------|
| $q_1$ | $\pi_1^c(E[a]), \pi_2^c(E[a])$  | $\pi_1^\ell, E[\pi_2^f(a)] - K$        | $\pi_1^\ell, \pi_2^f(E[a])$           |
| $M_1$ | $E[\pi_1^f(a)] - K, \pi_2^\ell$ | $E[\pi_1^c(a)] - K, E[\pi_2^c(a)] - K$ | $E[\pi_1^{Ic}(a)] - K, \pi_2^c(E[a])$ |
| $W_1$ | $\pi_1^f(E[a]), \pi_2^\ell$     | $\pi_1^c(E[a]), E[\pi_2^{Ic}(a)] - K$  | $\pi_1^c(E[a]), \pi_2^c(E[a])$        |

Table 2: The Payoffs of Equilibrium Candidates

Now we can use the reduced normal-form game in Table 1 to check whether the nine equilibrium candidates enumerated above are actually Nash equilibria. By Lemma 1, the NE of the reduced normal-form game give rise to the SPNE of the extensive-form game. Of course, the structure of the set of NE depends crucially on the market research cost  $K$ . The following three subsections discuss the cases with large, small, and intermediate  $K$ , respectively.

### 3.3 High Market Research Costs ( $K > \frac{1}{4}V[a]$ )

Clearly, the incentives for carrying out market research decrease as  $K$  increases. Intuitively, if the market research cost is high enough, it will offset the gains from obtaining accurate market information. A cutoff value is derived from the following proposition, above which waiting is always better than market research in the reduced normal-form game.

**Proposition 1.** *When  $K > \frac{1}{4}V[a]$ , conducting market research is strictly dominated by waiting in the reduced normal-form game, for both firms  $i \in \{1, 2\}$ . There are three pure-strategy SPNE: in one of the equilibria, both firms produce the Cournot-Nash equilibrium quantities in the first period. In the other two equilibria, firms behave as Stackelberg leader and follower respectively.*

The proofs of all propositions and theorems are relegated to the Appendix.

The fact that the cutoff value is related to the variance of market capacity is very intuitive, since the variance is a natural measure of the value of the information obtained through market research. According to Proposition 1, when  $K > \frac{1}{4}V[a]$ , the strictly dominated strategy, market research, can be eliminated in the reduced normal-form game. In this case, the model becomes a generalization of HS' model with action commitment, where market demand is allowed to be stochastic. Since firms are unable to update their information, each firm has the same strategic incentives as in a perfect information context. Hence, the equilibria are the same as those of the HS' action commitment model. This is the less interesting case for our analysis, because market research plays no role.

### 3.4 Low Market Research Costs ( $K < \frac{1}{9}V[a]$ )

A lower market research cost  $K$  increases the likelihood that a firm will carry out market research rather than waiting. In the extreme case with  $K = 0$ , market research is costless, which corresponds to Sadanand and Sadanand (1996). In this case, no firm would strictly prefer waiting if market research is feasible. In the next proposition, we find a cutoff value for  $K$ , below which carrying out market research always outperforms waiting.

**Proposition 2.** *When  $K < \frac{1}{9}V[a]$ , waiting is strictly dominated by market research in the reduced normal-form game, for both firms  $i \in \{1, 2\}$ .*

Again, the fact that the cutoff value is related to the variance of market capacity is very intuitive. For a large variance, information is very valuable and hence market research pays off.

Proposition 2 greatly simplifies the analysis whenever  $K < \frac{1}{9}V[a]$ . In this case, we can eliminate the strictly dominated strategy, waiting, in the reduced normal-form game. In order to find out the pure-strategy NE in the reduced normal-form game, only four equilibrium candidates remain. Table 3 shows the payoffs of these candidates.

|       | $q_2$                           | $M_2$                                  |
|-------|---------------------------------|--|
| $q_1$ | $\pi_1^c(E[a]), \pi_2^c(E[a])$  | $\pi_1^\ell, E[\pi_2^f(a)] - K$        |
| $M_1$ | $E[\pi_1^f(a)] - K, \pi_2^\ell$ | $E[\pi_1^c(a)] - K, E[\pi_2^c(a)] - K$ |

Table 3: The Payoffs of Equilibrium Candidates for  $K < \frac{1}{9}V[a]$

The next theorem summarizes the results.

**Theorem 1.** *Assume (1) and (2). When  $K < \frac{1}{9}V[a]$ , for any pure-strategy subgame-perfect Nash equilibrium  $(s_i^1, s_i^2)_{i=1,2}$ , second-period decisions are given by  $s_i^2 = \bar{s}_i^2$  as in Lemma 1. Furthermore:*

- (i) a SPNE with  $s^1 = (q_1^\ell, M_2)$  exists, if and only if  $c_1 \leq \frac{1}{2}(c_2 + E[a] - \beta)$ ;
- (ii) a SPNE with  $s^1 = (M_1, q_2^\ell)$  exists, if and only if  $c_2 \leq \frac{1}{2}(c_1 + E[a] - \beta)$ ;
- (iii) a SPNE with  $s^1 = (M_1, M_2)$  exists, if and only if  $c_1 \geq \frac{1}{2}(c_2 + E[a] - \beta)$ ;

where  $\beta = 2\sqrt{2}\sqrt{V[a] - 9K}$ . Note that the condition in (ii) implies the one in (i).

We now briefly discuss this result. First note that the theorem implies that, for  $K < \frac{1}{9}V[a]$ , the equilibrium candidate where both firms produce the imperfect-information Cournot-Nash equilibrium quantity  $q_i^c(E[a])$  in the first period cannot give rise to a SPNE. The reason is that for each firm  $i$ , the deviation from  $q_i^c(E[a])$  to  $M_i$  changes the firm's expected profit from  $\pi_i^c(E[a])$  to  $E[\pi_i^{Ic}(a)] - K$ . When  $K < \frac{1}{9}V[a]$ , this deviation pays off. In other words, the gains from market research offset the cost  $K$ .

Item (i) identifies the necessary and sufficient condition for the strategy profile, where firm 1 chooses to produce the Stackelberg leader quantity and firm 2 chooses to carry out market research in the first period, to be a SPNE. Clearly, firm 2 (the follower) will not deviate to any other quantities in the second period if market research is chosen, since  $\bar{s}_2^2$  prescribes the optimal output level. Nor will it deviate to producing in the first period, because the gains from market research, i.e. the expected gross profit of being a follower minus the expected profit from a first-period best response against the Stackelberg leader quantity of firm 1,

$$E[\pi_2^f(a)] - \pi_2(q_2^f(E[a])|q_1^l),$$

offsets the market research cost  $K$  in this case. On the other hand, firm 1 (the leader) will not deviate from  $q_1^l$  if it has chosen to produce in the first period. The inequality in (i) guarantees that it will also not deviate to carry out market research in order to form a perfect-information Cournot duopoly with firm 2. This inequality implies that the production cost of firm 1 should be low enough. The intuition is simply that firm 1's leadership entails a low production cost to pay the price of market uncertainty and prevent the deviation to low-cost market research. However, the more favorable market conditions are, the less efficient the leader must be for the condition to be fulfilled. To see this, simply note that the inequality in (i) implies that the maximal production cost of firm 1 that supports this SPNE is increasing in  $E(a)$  but decreasing in  $V[a]$ .

The reason for this last observation is simple. Given  $V[a]$ , the increment of  $\pi_1^l$  induced by  $E[a]$  is larger than the increment of  $E[\pi_1^c(a)] - K$ , the expected net profit of firm 1 when deviating to carrying out market research.<sup>11</sup> If  $E[a]$  is large enough, the expected profit gained through leading the market will be higher than that from market research. Given  $E[a]$ , firm 1's incentive to deviate from producing first diminishes as  $V[a]$  becomes smaller, because a low  $V[a]$  indicates a relatively stable market capacity (low uncertainty). For small  $V[a]$ , firm 1's prior belief in the market demand, without added market research, already enables firm 1 to earn a higher profit than that following market research.

In short, firm 1 prefers producing first, given that its opponent conducts market research, whenever its production is efficient enough, relative to market conditions, for the "first mover advantage" to dominate the "informational advantage" of market research. As a result, endogenous leadership with an efficient leader and an informed inefficient follower appears in the equilibrium path.

Item (ii) shows the necessary and sufficient condition for the converse situation to the one in (i) to be a SPNE, that is, endogenous leadership with an inefficient leader and an informed

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<sup>11</sup>Technically,  $\frac{\partial \pi_i^l}{\partial E[a]} = \frac{1}{4}(E[a] + c_j - 2c_i)$  and  $\frac{\partial}{\partial E[a]}(E[\pi_1^c(a)] - K) = \frac{2}{9}(c_j - 2c_i)$ . If  $i = 1$ , then  $\frac{\partial \pi_1^l}{\partial E[a]} - \frac{\partial}{\partial E[a]}(E[\pi_1^c(a)] - K) = \frac{2}{9}E[a] + \frac{1}{36}[(E[a] - c_1) + (c_2 - c_1)] > 0$ . If  $i = 2$ , then  $\frac{\partial \pi_2^l}{\partial E[a]} - \frac{\partial}{\partial E[a]}(E[\pi_1^c(a)] - K) = \frac{1}{36}c_1 + \frac{1}{18}(E[a] - c_2) + \frac{7}{36}E[a] > 0$ . When  $E[a] > 2c_i - c_{-i} + 2\sqrt{\frac{1}{5}(V[a] - 9K)}$ ,  $\pi_i^l$  is always larger than  $(E[\pi_i^c(a)] - K)$ .

efficient follower. Firm 2 (the inefficient firm) produces the Stackelberg leader quantity and firm 1 carries out market research in the first period. The analysis is analogous to that for (i). The follower will not deviate for the same reason given for (i). The leader will not deviate either, if its marginal cost is small enough. The only difference is that, for given  $c_1$  and  $c_2$ , market conditions need to be more favorable for the inefficient firm to assume the leader role than for the efficient one. This is implicit contained in the inequality in (ii). Comparing it to the inequality in (i), one finds that, *ceteris paribus*, it entails a higher  $E[a]$  or a lower  $V[a]$ . The reason is simply that firm 2, without carrying out market research, will suffer a higher loss than firm 1 for given market conditions, simply because it is less efficient. In other words, whenever an endogenous-leadership SPNE with an inefficient leader exists, there is also a SPNE with an efficient leader.

The SPNE with simultaneous production in the second period appears if the condition in item (iii) is fulfilled. This condition requires the marginal costs of both firms to be high enough, relative to market conditions. The reason is that inefficient firms will suffer large losses due to market uncertainty, hence both firms would like to carry out market research. It should be pointed out that for very unfavorable market conditions, even if both firms have relatively low costs, no firm will produce in the first period. To see this explicitly, note that the inequality implies that the minimal production cost of firm 1 that supports this SPNE is increasing in  $E[a]$  and decreasing in  $V[a]$ . For unfavorable market conditions, the information about demand becomes so important that both firms would like to investigate the market and assume both the market research cost  $K$  and the ensuing harsher competition (firms become Cournot duopolist forgoing the possibility to become Stackelberg leaders). That is, “informational advantage” dominates the “first mover advantage.”

Another way to interpret Theorem 1 is to take  $c_1$ ,  $c_2$  and  $E(a)$  as given and see how the market uncertainty affects the timing choices of the firms. Clearly, when the market research cost is low enough, if the market uncertainty is sufficiently small so that the inequality in item (ii) is fulfilled, the sequential plays with either firm to commit can appear in the equilibrium. If the uncertainty is intermediate, so that only the condition in item (i) is fulfilled, the sequential play where the low-cost firm commits is the unique equilibrium. Finally, if the uncertainty is sufficiently large, so that the condition in item (iii) is satisfied, both firms would choose to wait. This result is similar to that of Güth, Ritzberger, and van Damme (2004), where one party chooses to commit and the other to wait if the uncertainty is sufficiently small. A difference in technique is that, we simply use the variance of market capacity to evaluate the magnitude of uncertainty. In Güth, Ritzberger, and van Damme (2004), however, they propose a parametric condition on the distribution of the surplus size, so that if a certain parameter  $\varepsilon$  is sufficiently small, most of the mass is concentrated around the mean. Therefore, one can use  $\varepsilon$  to measure the uncertainty of the surplus size.

Figure 2 illustrates Theorem 1 using a numerical example. It shows the areas where the three possible SPNE exist, in the coordinate system of marginal costs for  $K < \frac{1}{9}V[a]$ . In this example,  $a$  follows a Bernoulli distribution taking the value  $a = 10$  with probability 0.7 and the value  $a = 20$  otherwise. The line through  $OCE$  represents the function  $c_1 = c_2$ . The line through  $BDE$  shows the function  $c_2 = \frac{1}{3}(2a^L - E[a] + 2c_1)$ . Since we assume (1) and (2), the relevant area is the triangle  $OEB$ . In this region, the line through  $CD$  is the function  $c_1 = \frac{1}{2}(c_2 + E[a] - \beta)$ . The line through  $AC$  shows the function  $c_2 = \frac{1}{2}(c_1 + E[a] - \beta)$ . According to Theorem 1, the strategy profile in which firm 1 produces first is a SPNE if  $c_1$  and  $c_2$  fall in the  $OCDB$  region. In the area  $OAC$ , the strategy profile in which firm 2 produces first is a SPNE. In the  $CDE$  region, the strategy profile where both firms carry out

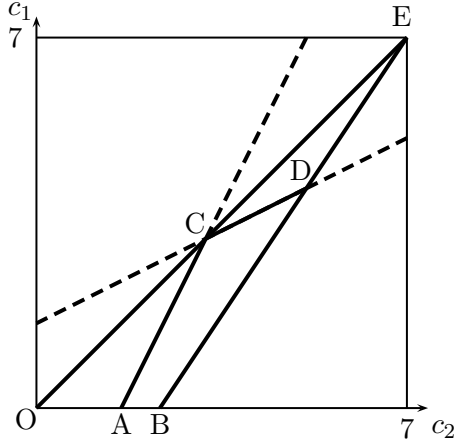


Figure 2: A numerical example for  $K < \frac{1}{9}V[a]$ . In this example,  $a$  is assumed to follow a Bernoulli distribution; that is with a probability of 0.7,  $a = 10$  and with a probability of 0.3,  $a = 20$ . Hence  $E[a] = 13$  and  $V[a] = 21$ . The market research cost is assumed to be 1.

market research is a SPNE. We see that if  $c_1$  and  $c_2$  are such that a SPNE with an inefficient leader exists, then the existence of a SPNE with an efficient leader follows automatically.

### 3.5 Intermediate Market Research Costs ( $\frac{1}{9}V[a] \leq K \leq \frac{1}{4}V[a]$ )

We now turn to the case of intermediate market research costs, i.e.  $\frac{1}{9}V[a] \leq K \leq \frac{1}{4}V[a]$ . In this case, no strategy is strictly dominated in the reduced normal-form game, thus we need to discuss all nine equilibrium candidates. We first explore the case with strict inequalities,  $\frac{1}{9}V[a] < K < \frac{1}{4}V[a]$ . This rules out the situations where waiting is weakly dominated by market research ( $K = \frac{1}{9}V[a]$ ) and where market research is weakly dominated by waiting ( $K = \frac{1}{4}V[a]$ ). Theorem 2 lists the SPNE for this scenario.

**Theorem 2.** *Assume (1) and (2). When  $\frac{1}{9}V[a] < K < \frac{1}{4}V[a]$ , there are two pure-strategy subgame-perfect Nash equilibrium, where second-period decisions are given by  $s_i^2 = \bar{s}_i^2$  as in Lemma 1, and the first-period decisions are  $(q_1^l, M_2)$  and  $(M_1, q_2^l)$  respectively.*

According to Theorem 2, two SPNE with endogenous leadership appear independently of the production costs. The leader, who produces  $q_i^l$ , will not deviate to waiting, because giving up leadership without obtaining accurate market information never pays off. Nor will it deviate to market research. The proof of Theorem 2 in the Appendix shows that the market research cost in this case is high enough to ensure that the deviation to market research is not worthwhile. The follower also has no incentive to deviate. As long as  $K < \frac{1}{4}V[a]$ , market research generates a higher profit than waiting, regardless of the quantity produced by the other firm in the first period (shown in the proof of Proposition 2). The follower has no incentive to deviate to producing the best reply to the leader's quantity in the first period either. The reason is that the gain from carrying out market research is the expected gross profit of the informed follower minus the expected profit of the uninformed follower, and this difference is larger than an intermediate market research cost (see inequality (30)).

The equilibrium candidate with simultaneous production in the first period is not a SPNE, as long as  $K < \frac{1}{4}V[a]$ . Given the imperfect-information Cournot-Nash equilibrium quantity of the opponent, one firm can benefit from market research, even though the market research cost is relatively high. We would also like to emphasize that, for  $K > \frac{1}{9}V[a]$ , none of the four equilibrium candidates with simultaneous production in the second period can be a NE. Neither  $(M_1, M_2)$  nor  $(W_1, W_2)$  can give rise to a SPNE, since both firms have an incentive to deviate to producing the Stackelberg leader quantity in the first period (shown in the proof of Theorem 2). Finally,  $(W_i, M_{-i}) \forall i \in \{1, 2\}$  cannot give rise to a SPNE, because as shown in the proof of Proposition 1 (equation (22)), the firm choosing market research always has incentive to deviate to wait when  $K > \frac{1}{9}V[a]$ .

Figure 3, generated by the same example as in Figure 2, illustrates the last result. All lines in this figure represent the same functions as in Figure 2. For instance, the line through  $BE$  shows the function  $c_2 = \frac{1}{3}(2a^L - E[a] + 2c_1)$  in the region  $c_1 \leq c_2$ . The two SPNE with endogenous leadership appear in the area  $OBE$ .

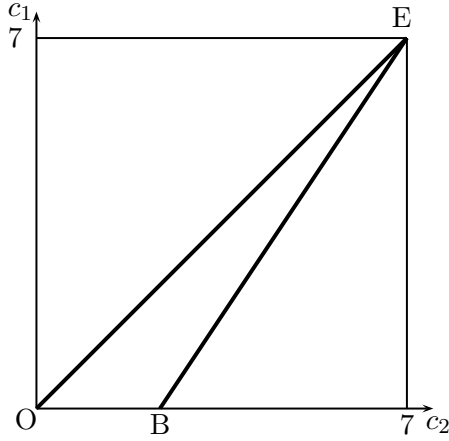


Figure 3: A numerical example for  $\frac{1}{9}V[a] < K < \frac{1}{4}V[a]$ .

Consider now the knife-edge scenarios where  $K = \frac{1}{9}V[a]$  or  $K = \frac{1}{4}V[a]$ . In both cases, we have payoff ties and hence firms are indifferent among two choices. For  $K = \frac{1}{9}V[a]$ , all the SPNE in Theorems 1 and 2 remain valid. Further, in this case  $\pi_i(W_i|M_{-i}) = \pi_i(M_i|M_{-i}), \forall i \in \{1, 2\}$  and it follows that  $(W_i, M_{-i}) \forall i \in \{1, 2\}$  are equilibria, which give rise to two SPNE with simultaneous production in the second period. For  $K = \frac{1}{4}V[a]$ , all the SPNE in Proposition 1 and Theorem 2 remain valid.

## 4 The Model with Observable Delay

We now turn our attention to the model structure with observable delay. Within this framework, players first announce when they will take actions, which becomes common knowledge before actions are really taken. Then, players move according to their announcements.

In our model, we assume that there is an initial stage, where firms announce whether they will produce in the first period (but not how much), carry out market research, or just wait and see. The announcements become public information, and then firms implement what

they have announced in the following two periods. As in the model with action commitment, the information on market demand is revealed only if a firm carries out market research.

This gives rise to an extensive-form game with nine subgames, which include simultaneous production in the first (second) period with (without) market research and sequential plays with (without) market research, as shown in section 3.2. Using backward induction, we can solve for the equilibria in all the subgames to obtain the following reduced normal-form game, where  $\text{Prod}_i$  ( $i = 1, 2$ ) denotes the announcement to produce in the first period.

|                 | $\text{Prod}_2$                 | $M_2$                                  | $W_2$                                 |
|-----------------|---------------------------------|--|---------------------------------------|
| $\text{Prod}_1$ | $\pi_1^c(E[a]), \pi_2^c(E[a])$  | $\pi_1^\ell, E[\pi_2^f(a)] - K$        | $\pi_1^\ell, \pi_2^f(E[a])$           |
| $M_1$           | $E[\pi_1^f(a)] - K, \pi_2^\ell$ | $E[\pi_1^c(a)] - K, E[\pi_2^c(a)] - K$ | $E[\pi_1^{Ic}(a)] - K, \pi_2^c(E[a])$ |
| $W_1$           | $\pi_1^f(E[a]), \pi_2^\ell$     | $\pi_1^c(E[a]), E[\pi_2^{Ic}(a)] - K$  | $\pi_1^c(E[a]), \pi_2^c(E[a])$        |

Table 4: The Reduced Normal-form Game with Observable Delay

Clearly,  $W_i$  is strictly dominated by  $\text{Prod}_i$ , for  $i = 1, 2$ , because  $\pi_i^f > \pi_i^c(E[a]) > \pi_i^f(E[a])$  for  $i = 1, 2$ . Therefore, wait can never be an equilibrium strategy in this game, regardless of market research cost. Eliminating the strictly dominated strategy, we only have to consider the first two strategies in the payoff matrix above.

The relationship between  $\pi_i^c(E[a])$  and  $E[\pi_i^f(a)] - K$  is important for the results. A straightforward computation shows that  $\pi_i^c(E[a]) \leq E[\pi_i^f(a)] - K$ ,  $i = 1, 2$ , if and only if

$$(c_i - 2c_j + E[a])(17c_i - 10c_j - 7E[a]) \geq 144K - 36V[a] \quad (19)$$

with  $i \neq j$ , while  $\pi_i^c(E[a]) \geq E[\pi_i^f(a)] - K$  if and only if the converse holds with  $\geq$ .

By the assumption on  $c_2$ , if  $K \geq \frac{1}{4}V[a]$ , conditions (19) always hold for both  $i = 1$  and  $j = 1$ . To see this, just notice that when  $c_2 < \frac{1}{3}(2a^L - E[a] + 2c_1)$ ,  $c_i - 2c_j + E[a] > 0$  and  $17c_i - 10c_j - 7E[a] < 0$  for  $i = 1, 2$ , while if  $K \geq \frac{1}{4}V[a]$ ,  $144K - 36V[a] \geq 0$ . This is very intuitive, as no one would like to carry out market research if  $K$  is too high. Furthermore, both conditions show that large market uncertainty gives firms incentive to market research, while small uncertainty leads firms to produce in the first period.

Comparing the payoffs in the matrix above, we can obtain the NE of the reduced normal-form game, which are summarized in the following theorem.

**Theorem 3.** *Consider the game of observable delay. The NE of the reduced normal-form game (and hence the announcements in the SPNE of the original game) are the following:*

I. when  $K \geq \frac{1}{4}V[a]$ ,  $(\text{Prod}_1, \text{Prod}_2)$ .

II. when  $K \leq \frac{1}{9}V[a]$ ,

i.  $(M_1, M_2)$  whenever  $c_1 \geq \frac{1}{2}(E[a] + c_2 - \beta)$ .

ii.  $(\text{Prod}_1, \text{Prod}_2)$ , whenever the converse of condition (19) holds for both  $i = 1$  and  $j = 1$ .

iii.  $(M_1, \text{Prod}_2)$  whenever  $c_2 \leq \frac{1}{2}(E[a] + c_1 - \beta)$  and condition (19) holds for  $i = 1$ .



iv.  $(Prod_1, M_2)$  whenever  $c_1 \leq \frac{1}{2}(E[a] + c_2 - \beta)$  and condition (19) holds for  $i = 2$ .

III. when  $\frac{1}{9}V[a] < K < \frac{1}{4}V[a]$ ,

i.  $(Prod_1, Prod_2)$ , whenever the converse of condition (19) holds for both  $i = 1$  and  $j = 1$ ;

ii.  $(M_1, Prod_2)$ , whenever condition (19) holds for  $i = 1$ ;

iii.  $(Prod_1, M_2)$ , whenever condition (19) holds for  $i = 2$ .

It is very intuitive that when  $K$  is sufficiently high, both firms will choose to produce simultaneously in the first period. This result corresponds to that of HS' game of observable delay, where market demand is fixed and any positive research cost will be too high. In contrast, when  $K$  is sufficiently low, each of the four strategy profiles can be equilibrium in the reduced normal-form game, depending on production costs and market uncertainty. If  $K$  is intermediate, there is no equilibrium where both firms carry out market research simultaneously, because the payoff of the Cournot outcome with market research is always lower than that of the leader without market research as long as  $K > \frac{1}{9}V[a]$ . Moreover, if  $K$  is not too high, Stackelberg results appear in the equilibrium, where, for a relatively poor market condition, the efficient firm is more likely to become a leader. Finally, if production costs of both firms are low relative to market uncertainty, both firms will choose to produce in the first period.

## 5 Discussion

Real-world firms always face a certain degree of uncertainty about market demand. This creates an incentive for market research. In the previous literature on firms' endogenous timing choices, firms either face a deterministic market demand (e.g. HS), have predetermined asymmetric information (Mailath (1993) and Normann (2002)), or can automatically update information without any cost (e.g. Sadanand and Sadanand (1996)). Daughety and Reinganum (1994) does make information acquisition costly, however, the whole procedure of market research is simplified as an one-shot trade for information, leaving no room for the choice between market research and production.

This paper develops two endogenous timing models, which help understand the appearance of endogenous leadership or simultaneous production when market research explicitly plays a role. The first model is an extension of HS' action commitment model allowing for stochastic market demand and information updating and also similar to Sadanand and Sadanand (1996) and Güth, Ritzberger, and van Damme (2004), except for the fact that information acquisition is *costly*. The second model is built on HS' game of observable delay. The models of HS and Sadanand and Sadanand (1996) are encompassed in the present models as particular cases (see below).

Our models provide a new explanation for the appearance of endogenous leadership or simultaneous production. Namely, market research induces a trade-off between the "informational advantage" and the "first mover advantage", which eventually determines firms' timing choices. If a firm decides to produce in the first period, it has a chance to obtain the "first mover advantage" but lose the "informational advantage". The converse is true for a firm carrying out market research and producing later.

The model of action commitment delivers clear-cut predictions in a variety of parameter constellations. When the market research cost is small, there is a unique SPNE with simultaneous production in the second period, provided production costs of both firms are high and market capacity has a small expectation and large variance. For the same level of market research costs, if the production cost of the efficient firm is small enough but that of inefficient one is large, there is a unique pure-strategy SPNE with the efficient firm as endogenous leader, as long as market capacity has a relatively small expectation and large variation, so that only the efficient firm can be the leader. For intermediate values of  $K$ , simultaneous production does not appear in equilibrium; only two pure-strategy SPNE with endogenous leadership exist, independently of production costs. When  $K$  is large, there are two SPNE with Stackelberg outcomes, wherein the follower chooses to wait in period 1. Besides, there is a SPNE with Cournot outcome in period 1.

The model of action commitment generalizes several results in the related literature. HS' action commitment model can be treated as a particular case of our model when market research cost is high (i.e.  $K \geq \frac{1}{4}V[a]$ ). The reason is that when there is no market uncertainty, any  $K > 0$  is too large. Hence, in HS' model, there are two SPNE where one firm choose to wait and the other firm chooses to produce in the first period and a SPNE where both firms produce simultaneously in the first period. In Sadanand and Sadanand (1996)'s symmetric model, the revelation of information is costless, hence it becomes a special case of our model where  $K = 0$ . Therefore, in this model, there are two pure-strategy SPNE with Stackelberg outcomes when the market uncertainty is small and a unique pure-strategy SPNE where both firms choose to produce in the second period when the uncertainty is large, corresponding to the case where  $K \leq \frac{1}{9}V[a]$  in our model.

Moreover, this result is also comparable to Güth, Ritzberger, and van Damme (2004)'s action commitment model, although they concern a bargaining game. They show that, if market research cost is sufficiently low (in their model  $K = 0$ ) and the information uncertainty is also sufficiently small, sequential plays appear in the equilibria, which is exactly consistent with our result summarized in Theorem 1. The mechanism leading to their result is also analogous to us. In their model, both parties committing could not be an equilibrium, since one can always choose waiting to avoid the risk and collect the residual. Both parties choosing to wait could not be an equilibrium either, since deviating to pre-commitment can always generate higher payoff, as long as the uncertainty is sufficiently small. Therefore, only sequential plays survive as equilibria.

Furthermore, our result are parallel to Hirokawa and Sasaki (2001) to some extent, although the mechanisms behind both models are different. In our model, there are only two periods and the market clears at the end of period 2. The equilibrium timing, essentially, is determined by market uncertainty *relative to* the market research cost. In their model, there are infinitely many periods and markets clear at the end of each period. As a result, the equilibrium timing is determined by market uncertainty *relative to* the inverse of the discount factor. Nonetheless, we share very comparable results. When *relative* market uncertainty (although relative to different references in the two models) is small (i.e. case 1 in our model where  $V[a] \leq 4K$ ), both firms entering simultaneously in period 1 results in a SPNE. When *relative* uncertainty is large (i.e. case 2 in our model where  $V[a] \geq 9K$ ), Stackelberg outcome appears in equilibrium.

In our model, however, when relative uncertainty is small, Stackelberg outcome also appears in equilibrium, which, in contrast, does not hold in Hirokawa and Sasaki (2001), because, with a relatively small discount factor and small market uncertainty, firms will be worse off

if they change to produce as followers. When uncertainty is relatively large, in our model, both firms carrying out market research and producing simultaneously in period 2 results in a SPNE. But this can never lead to a SPNE in Hirokawa and Sasaki (2001). Since they assume that market information becomes observable only if at least one firm enters the market and firms cannot adjust their output levels once decided in the first production period. Hence, if both firms decide to simultaneously produce later, market information is still unavailable in their first production period, which leads to large losses, so that delaying production becomes more profitable.

Finally, in the model of observable delay, the results crucially depend on parameters, i.e. production costs, market research cost and market condition. When  $K \geq \frac{1}{4}V[a]$ , we obtain the same result as in HS, i.e. simultaneous production in the first period, since HS' model of observable delay without market uncertainty is a particular case of ours. Simultaneous market research can occur in a SPNE only if  $K \leq \frac{1}{9}V[a]$ , since for any larger  $K$ , Stackelberg leadership always leads to higher payoff. Sequential plays can be equilibria when  $K < \frac{1}{4}V[a]$ . If market uncertainty is small even relative to the less efficient firm, either firm can be a leader. But if the uncertainty is small only in terms of the efficient firm, only the efficient firm can be a leader.

## Appendix

### Proof of Proposition 1

*Proof.* Let  $K > \frac{1}{4}V[a]$ . We want to show that market research is strictly dominated by waiting in the reduced normal-form game. Denote by  $\pi_i(\cdot|\cdot)$  the payoffs in this game (as given in Table 1).

Suppose first that firm  $-i$  chooses some output level  $s_{-i}^1 \in \mathbb{R}^+$  in the first period. Firm  $i$  strictly prefers  $W_i$  rather than  $M_i$  if and only if

$$\begin{aligned} & \pi_i(W_i|q_{-i}^1) > \pi_i(M_i|q_{-i}^1) \\ \Leftrightarrow & \frac{1}{4}(E[a] - s_{-i}^1 - c_i)^2 > E\left[\frac{1}{4}(a - s_{-i}^1 - c_i)^2\right] - K \\ \Leftrightarrow & K > \frac{1}{4}V[a] \end{aligned} \tag{20}$$

Second, if firm  $-i$  decides to wait,  $W_i$  is strictly better than  $M_i$  for firm  $i$  if and only if

$$\begin{aligned} & \pi_i(W_i|W_{-i}) > \pi_i(M_i|W_{-i}) \\ \Leftrightarrow & E\left[\frac{(E[a] + c_{-i} - 2c_i)^2}{9}\right] > \frac{1}{36}E[(3a - E[a] - 4c_i + 2c_{-i})^2] - K \\ \Leftrightarrow & K > \frac{1}{4}V[a] \end{aligned} \tag{21}$$

Last, if firm  $-i$  conducts market research, then for firm  $i$ ,  $W_i$  is strictly preferred to  $M_i$  if and only if

$$\begin{aligned} & \pi_i(W_i|M_{-i}) > \pi_i(M_i|M_{-i}) \\ \Leftrightarrow & \frac{1}{9}(E[a] + c_i - 2c_{-i})^2 > E\left[\frac{(a + c_{-i} - 2c_i)^2}{9}\right] - K \\ \Leftrightarrow & K > \frac{1}{9}V[a] \end{aligned} \tag{22}$$

Combining conditions (20), (21) and (22), if  $K > \frac{1}{4}V[a]$ , market research is strictly dominated by waiting (for both firms) in the reduced normal-form game.  $\square$

## Proof of Proposition 2

*Proof.* The proof follows from conditions (20), (21) and (22), simply reversing all inequalities. It follows that, if  $K < \frac{1}{9}V[a]$ , waiting is strictly dominated by market research (for both firms) in the reduced normal-form game.  $\square$

## Proof of Theorem 1

*Proof.* We look for all the pure-strategy Nash equilibria for  $K < \frac{1}{9}V[a]$  in the reduced normal-form game. We only need to check which of the four equilibrium candidates, shown in Table 3, are actually Nash equilibria.

*Both firms produce  $q_i^c(E[a])$  in the first period.* When each firm uses this strategy, the expected profit of firm  $i$  is  $\pi_i^c(E[a])$ . Since waiting is strictly dominated by market research according to Proposition 2, we only need to check whether a deviation to  $M_i$  would pay off. This deviation would enable firm  $i$  to adopt the best response to its opponent's quantity  $q_{-i}^c(E[a])$  in each state  $a \in [a^L, a^H]$ ,

$$BR_i(a, q_{-i}^c(E[a])) = q_i^{Ic}(a) = \frac{1}{6}(3a - E[a] + 2c_{-i} - 4c_i) \quad (23)$$

Hence the expected net profit of firm  $i$  would be  $E[\pi_i^{Ic}(a)] - K$ . Thus,  $(q_i^c(E[a]), q_{-i}^c(E[a]))$  is a NE if and only if  $\pi_i^c(E[a]) \geq E[\pi_i^{Ic}(a)] - K$  for both  $i \in \{1, 2\}$ . That is,

$$\begin{aligned} & \pi_i^c(E[a]) - E[\pi_i^{Ic}(a)] + K \geq 0 \\ \Leftrightarrow & \frac{1}{9}(E[a] + c_{-i} - 2c_i)^2 - \frac{1}{36}E[(3a - E[a] + 2c_{-i} - 4c_i)^2] + K \geq 0 \\ \Leftrightarrow & K \geq \frac{1}{4}V[a] \end{aligned} \quad (24)$$

Therefore, when  $K < \frac{1}{9}V[a]$ , both firms have incentive to deviate to market research. It follows that  $(q_i^c(E[a]), q_{-i}^c(E[a]))$  is not a NE in the reduced normal-form game.

*Firm 1 produces  $q_1^\ell$  and firm 2 chooses  $M_2$  in the first period.* The profits of firm 1 when producing  $q_1^\ell$  are  $\pi_1^\ell$ . Again, the best deviation of firm 1 is to choose  $M_1$ , which, given that firm 2 chooses  $M_2$ , results in a perfect-information Cournot duopoly in the second period and generates the expected net profit  $E[\pi_1^c(a)] - K$  for firm 1. Therefore, firm 1 will have no incentive to deviate from  $q_1^\ell$  to  $M_1$  if and only if  $\pi_1^\ell \geq E[\pi_1^c(a)] - K$ . That is,

$$\begin{aligned} & \frac{1}{8}(E[a] - 2c_1 + c_2)^2 \geq E\left[\frac{1}{9}(a - 2c_1 + c_2)^2\right] - K \\ \Rightarrow & 9(E[a] - 2c_1 + c_2)^2 - 8E[(a - 2c_1 + c_2)^2] + 72K \geq 0 \\ \Rightarrow & (2c_1 - c_2)^2 - 2E[a](2c_1 - c_2) + E[a]^2 \geq 8V[a] - 72K \\ \Rightarrow & (2c_1 - c_2 - E[a])^2 \geq 8(V[a] - 9K) \end{aligned} \quad (25)$$

For  $K \leq \frac{1}{9}V[a]$ , the last inequality holds if and only if

$$c_1 \leq \frac{1}{2}\left(E[a] + c_2 - 2\sqrt{2}\sqrt{V[a] - 9K}\right) \quad \text{or} \quad (26)$$

$$c_1 \geq \frac{1}{2}\left(E[a] + c_2 + 2\sqrt{2}\sqrt{V[a] - 9K}\right) \quad (27)$$

Inequality (27) implies that  $c_1 > c_2$ , which contradicts the assumption that  $c_1 \leq c_2$ . Thus, inequality (26) is the necessary and sufficient condition for firm 1 not to have an incentive to deviate from  $q_1^\ell$ .

The expected net profit of firm 2 when choosing  $M_2$  is  $E[\pi_2^f(a)] - K$ . If firm 2 deviates to producing in the first period, the optimal quantity is given by

$$BR_2(q_1^\ell) = q_2^f(E[a]) = \frac{1}{4}(E[a] - 3c_2 + 2c_1) \quad (28)$$

which generates the expected profit

$$\pi_2(q_2^f(E[a])|q_1^\ell) = \frac{1}{16}(E[a] - 3c_2 + 2c_1)^2 \quad (29)$$

Hence, firm 2 will have no incentive to deviate if and only if

$$\begin{aligned} E[\pi_2^f(a)] - K &\geq \pi_2(q_2^f(E[a])|q_1^\ell) \\ \Leftrightarrow E \left[ \frac{(2a - E[a] - 3c_2 + 2c_1)^2}{16} \right] - K - \frac{1}{16}(E[a] - 3c_2 + 2c_1)^2 &\geq 0 \\ \Leftrightarrow K &\leq \frac{1}{4}V[a] \end{aligned} \quad (30)$$

Since we assume  $K < \frac{1}{9}V[a]$  here, firm 2 will not deviate from  $M_2$ . Hence, when  $K < \frac{1}{9}V[a]$ , the strategy profile  $(q_1^\ell, M_2)$  is a NE in the reduced normal-form game if and only if (26) is satisfied.

*Firm 2 produces  $q_2^\ell$  and firm 1 carries out market research in the first period.* This situation is analogous to the previous one. Firm 2 (the leader) will not have an incentive to deviate if  $\pi_2^\ell \geq E[\pi_2^c(a)] - K$ . When  $K < \frac{1}{9}V[a]$ , this condition holds if and only if

$$c_2 \leq \frac{1}{2} \left( E[a] + c_1 - 2\sqrt{2}\sqrt{V[a] - 9K} \right) \quad \text{or} \quad (31)$$

$$c_2 \geq \frac{1}{2} \left( E[a] + c_1 + 2\sqrt{2}\sqrt{V[a] - 9K} \right) \quad (32)$$

Inequality (32) implies that  $c_2 > \frac{1}{2}(E[a] + c_1)$ , which contradicts our assumption that  $c_2 < \frac{1}{3}(2a^L - E[a] + 2c_1) < \frac{1}{2}(E[a] + c_1)$  (it would imply a negative  $q_2^f(E[a])$ ). Hence, inequality (31) is the necessary and sufficient condition for firm 2 not to deviate from  $q_2^\ell$ .

Firm 1 (the follower) will not have an incentive to deviate if its profits as a follower are larger than or equal to the profit from taking a best reply against  $q_2^\ell$  without market research, i.e. if  $\pi_1^\ell \geq \pi_1(q_2^f(E[a])|q_2^\ell)$ . This condition holds if and only if  $K \leq \frac{1}{4}V[a]$ . Thus when  $K < \frac{1}{9}V[a]$  firm 1 will not deviate. The strategy profile  $(M_1, q_2^\ell)$  is a NE in the reduced normal-form game if and only if condition (31) is satisfied.

*Both firms carry out market research in the first period.* In this case, the expected profit of each firm  $i$  is  $E[\pi_i^c(a)] - K$ . The best deviation of firm  $i$ , given its opponent chooses  $M_{-i}$ , is to produce  $q_i^\ell$  in the first period. Firm  $i$  will not have an incentive to deviate if  $E[\pi_i^c(a)] - K \geq \pi_i^\ell$  for each  $i \in \{1, 2\}$ . That is,

$$\begin{aligned} E \left[ \frac{1}{9}(a - 2c_i + c_{-i})^2 \right] - K &\geq \frac{1}{8}(E[a] - 2c_i + c_{-i})^2 \\ \Rightarrow 8E[(a - 2c_i + c_{-i})^2] - 72K - 9(E[a] - 2c_i + c_{-i})^2 &\geq 0 \\ \Rightarrow (2c_i - c_{-i} - E[a])^2 &\leq 8(V[a] - 9K) \end{aligned} \quad (33)$$

For  $K < \frac{1}{9}V[a]$ , this condition holds if and only if

$$\frac{1}{2}(E[a] + c_2 - \beta) \leq c_1 \leq \frac{1}{2}(E[a] + c_2 + \beta) \quad \text{and} \quad (34)$$

$$\frac{1}{2}(E[a] + c_1 - \beta) \leq c_2 \leq \frac{1}{2}(E[a] + c_1 + \beta) \quad (35)$$

The RHS of equation (34) is (weakly) larger than that of equation (35), because  $c_1 \leq c_2$ . Recalling our assumption on the positivity of all relevant quantities (i.e.  $c_2 < \frac{1}{3}(2a^L - E[a] + 2c_1)$ ), and the fact that  $\frac{1}{3}(2a^L - E[a] + 2c_1) - \frac{1}{2}(E[a] + c_1) = -\frac{1}{6}(4a^L + c_1 - 5E[a]) \leq 0$ , we see that  $c_2 \leq \frac{1}{2}(E[a] + c_1 + \beta)$  is automatically fulfilled. It is also easy to verify that the LHS of equation (34) is (weakly) larger than that of equation (35). Since  $c_1 \leq c_2$ , we conclude that (34) and (35) are fulfilled if and only if

$$c_1 \geq \frac{1}{2}(E[a] + c_2 - \beta).$$

□

## Proof of Theorem 2

*Proof.* We want to prove that, for  $\frac{1}{9}V[a] < K < \frac{1}{4}V[a]$ , the only SPNE correspond to the two equilibrium candidates with endogenous leadership in the reduced normal-form game, independently of  $c_1$  and  $c_2$ .

Suppose firm  $i$  produces  $q_i^\ell$  and firm  $-i$  chooses  $M_{-i}$  in the first period, where  $i \in \{1, 2\}$ . Firm  $-i$  will not have an incentive to deviate to producing in the first period as long as its profits as informed follower are larger than or equal to the profits from adopting a best response to  $q_i^\ell$  in the first period, i.e.  $E[\pi_{-i}^f(a)] - K \geq \pi_{-i}(q_{-i}^f(E[a])|q_i^\ell)$ . As shown in (30) in the proof of Theorem 1, this inequality holds if and only if  $K \leq \frac{1}{4}V[a]$ . The proof of Proposition 1 shows that, for  $K < \frac{1}{4}V[a]$ , market research always generates higher profits than wait, for any output level of the leader. Hence, firm  $-i$  has no incentive to deviate to  $W_{-i}$  either.

Firm  $i$  will not have an incentive to deviate from  $q_i^\ell$  to  $M_i$  if its expected profits as leader are larger than or equal to the expected net profit generated by market research, i.e. if  $\pi_i^\ell \geq E[\pi_i^c(a)] - K$ . This condition is always fulfilled for  $K \geq \frac{1}{9}V[a]$ . To see this, note that the expected profit difference

$$\pi_i^\ell - (E[\pi_i^c(a)] - K) = \frac{1}{8}[E[a] + c_{-i} - 2c_i]^2 - \frac{1}{9}E[(a + c_{-i} - 2c_i)^2] + K \quad (36)$$

is an increasing function of  $K$  and, for  $K = \frac{1}{9}V[a]$ , attains the value

$$\pi_i^\ell - E[\pi_i^c(a)] = \frac{1}{72}(E[a] - 2c_i + c_{-i})^2 \geq 0 \quad (37)$$

independently of  $c_i \forall i \in \{1, 2\}$ . Thus firm  $i$  has no incentive to deviate to market research for  $\frac{1}{9}V[a] < K < \frac{1}{4}V[a]$ . It will not deviate to wait if  $\pi_i^\ell \geq \pi_i^c(E[a])$  either, because

$$\pi_i^\ell = \frac{1}{8}(E[a] - 2c_i + c_{-i})^2 < \frac{1}{9}(E[a] - 2c_i + c_{-i})^2 = \pi_i^c(E[a]). \quad (38)$$

We conclude that the strategy profiles  $(q_i^\ell, M_{-i})$  for both  $i \in \{1, 2\}$  are NE of the reduced-form game.

None of the strategy profiles with simultaneous production in the second period is a NE for  $\frac{1}{9}V[a] < K < \frac{1}{4}V[a]$ . Let us start with  $(M_1, M_2)$ . As shown in (36) and (37) above,  $E[\pi_i^c(a)] - K < \pi_i^\ell$  for  $K > \frac{1}{9}V[a]$ . Thus both firms have an incentive to deviate to  $q_i^\ell$ . The profile  $(W_1, W_2)$  is not a NE either, because by (38) above firms have an incentive to deviate to producing  $q_i^\ell$ . The profiles  $(W_i, M_{-i}) \forall i \in \{1, 2\}$  are not NE either, because the waiting firm has an incentive to deviate to  $q_i^\ell$ , since  $\pi_i^\ell > \pi_i^c(E[a])$  by (38).

Finally, we have to prove that  $(q_i^c(E[a]), q_{-i}^c(E[a]))$  is not a NE for  $\frac{1}{9}V[a] < K < \frac{1}{4}V[a]$ . This is immediate from (24) in the proof of Theorem 1, which implies that deviating to market research pays off if  $K < \frac{1}{4}V[a]$ .  $\square$

### Proof of Theorem 3

*Proof.* The NE in the reduced normal-form game are obtained by comparing the payoffs in table 4. The relationship between  $\pi_i^c(E[a])$  and  $E[\pi_i^f(a)] - K$  is determined by condition (19). The relationship between  $\pi_i^\ell$  and  $E[\pi_i^c(a)] - K$  is shown by condition (26) and (27). Given those conditions, one can easily compare the payoffs and obtain the results in the statement.  $\square$

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